Tensile Strength of Short Headed Anchors Embedded in Steel Fibrous Concrete

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ABSTRACT

This paper deals with the tensile behaviour and strength of cast-in-place short headed anchor bolts embedded in both normal concrete (NC) and steel fibre reinforced concrete (SFRC). Four volume fractions (v_f =0.4%, 0.8%, 1.2%, and 1.6%), two aspect ratios (l_f / d_f =19.63, 36.33), three bolt diameters (d_b =8, 10, 12mm), and four embedment depths (h_{ef} =25, 37.5, 50, 62.5mm) were used. More than (108) specimens were tested under monotonic tensile loading. Only (90) specimens were failed by large concrete failure cone exceeding the dimensions of the specimen and the cone breaks into pieces in most cases (concrete failure), while the other specimens were failed by yielding or fracture of the bolts (steel failure). Tests results showed that breakout capacity (P_u) of the anchors were significantly enhanced by the addition of steel fibers to concrete and the size of the failure cone in (SFRC) specimens were smaller than the size of failure cones in (NC).

Key word: Breakout capacity, cast-in-place, failure cone, headed anchor bolt, pullout test, steel fibers.

مقاومة الشد للمثبتات القصيرة ذات الرؤوس المطمورة في خرسانة ليفية فولاذية

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الخلاصة

يتضمن هذا البحث دراسة مقاومة وسلوك الشد للبراغي القصيرة ذات الرؤوس المطمورة في خرسانة عادية وخرسانة مسلحة بالالياف الفولاذية. استعملت اربع نسب للالياف الفولاذية (0.4%، 0.8%، 1.2%، و1.6%)، نسبتين باعيتين للالياف (19.63 و 36.33)، ثلاثة اقطار للبراغي (8،   10، و 12 mm)، واربعة اعماق دفن (25، 37.5، 50، و 62.5mm). تم تحضير أكثرمن 108 نموذج وفحصت تحت تأثير حمل شد متزايد. فشلت 90 من النماذج فقط على شكل مخروط خرساني زادت ابعاده عن ابعاد النماذج وانقسم المخروط الى عدة أجزاء في معظم الحالات، بينما فشلت النماذج الاخرى بانقطاع البرغي (فشل الحديد). أظهرت النتائج أن مقاومة الشد للبراغي تتحسن بشكل ملحوظ باضافة الالياف الفولاذية وان حجم المخروط الخرساني أقل في الخرسانة الليفية عما هوعليه في الخرسانة الاعتيادية.

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INTRODUCTION

Anchor bolts embedded in concrete are found in many kinds of structures, and are subjected to different load combinations. A short anchor bolt is usually defined as one whose embedment length is insufficient to develop tensile yield in the bolt without the end anchorage provided by the bolt head [1]. The anchors can be used for attachments of instruments, and other structural members to concrete, as well as many other uses in structural applications (precast, prestressed, etc.). Anchors can be classified according to the way of installation, namely post-installed, and cast-in-place [2,3].
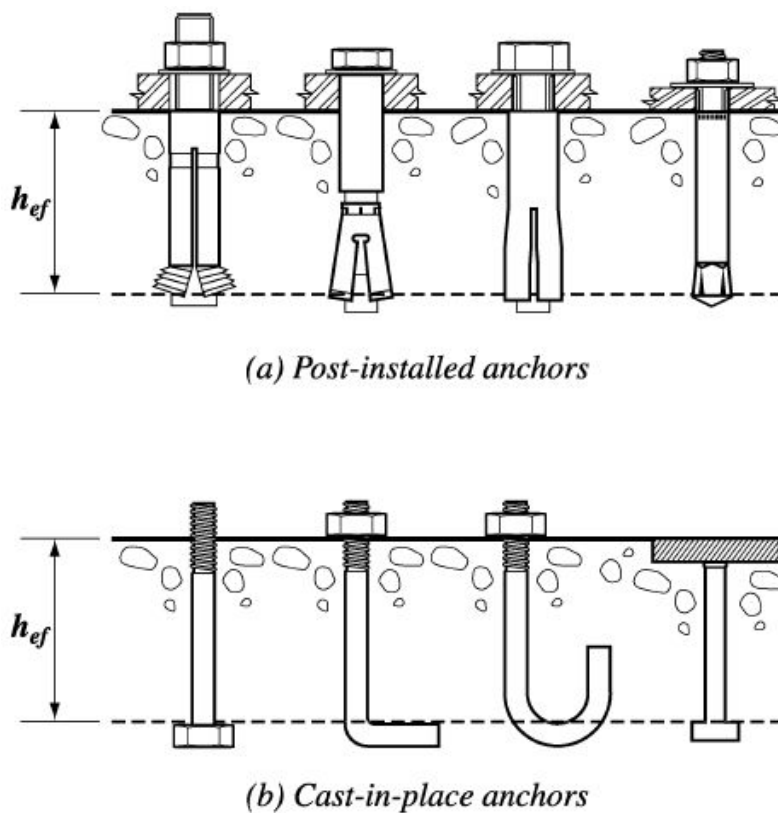
Fig. (1) Types of anchors, (a) Post-installed anchors, (b) Cast-in-place anchors [1]

Post-installed anchors can be fastened in almost any position desired in hardened concrete by installing them in a hole drilled after concrete hardening, and these may include expansion and undercut anchors whereby the load transfer to concrete is achieved

by bearing against the head. Adhesive and grouted anchors which transfer loads by bond between the fastener and concrete can also be used, Fig. (1a).

Cast-in place installed systems are available for fastening to the formwork before casting the fresh concrete in the formwork, and these include headed anchor bolts, headed studs, J or L bolts, and undercut anchors. These anchors transfer loads to the concrete by bond (friction and mechanical interlocking) and bearing against the head, Fig. (1b).

It has been found that the pull-out capacity of short headed anchor bolts embedded in normal concrete is proportional to the tensile strength of concrete, and nonlinearly to the embedment depth of the anchor [1-4].

Addition of steel fibers to concrete improves the tensile strength, strain capacity, ductility, and fracture toughness [4,5], thus anchors behaviour and strength may be different in (SFRC) than in (NC).

REASERCH SIGNIFICANCE

The aim of this experimental programme is to study the effect of adding short discrete steel fibers on the tensile strength and behaviour of short headed anchors embedded in concrete.

EXPERIMENTAL PROGRAM

Figure (2) shows the flowchart of the experimental programme [6]. The specimens were divided into four groups depending on the embedment depth, (25, 37.5, 50, 62.5mm). For each group three bolt diameters were used (d_b=8, 10, 12mm). Two aspect ratios of the steel fibers were used, and for each one, five fibers volume percentages were used (v_f =0, 0.4. 0.8, 1.2, 1.6). With each specimen, six cylinders (100×200mm) were cast; three for measuring the compressive strength and three for the splitting tensile strength.

Steel: Three diameters of the anchor bolts were used (d_b =8, 10, 12mm). Table (1) shows the engineering properties of the anchor bolts. Steel reinforcement with (8mm) diameter was used to reinforce the periphery of the specimens in the longitudinal and

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circumferential directions to prevent tension failure in concrete, and bars with (16mm) diameter were used to support the specimens in the test apparatus, Fig.(3).
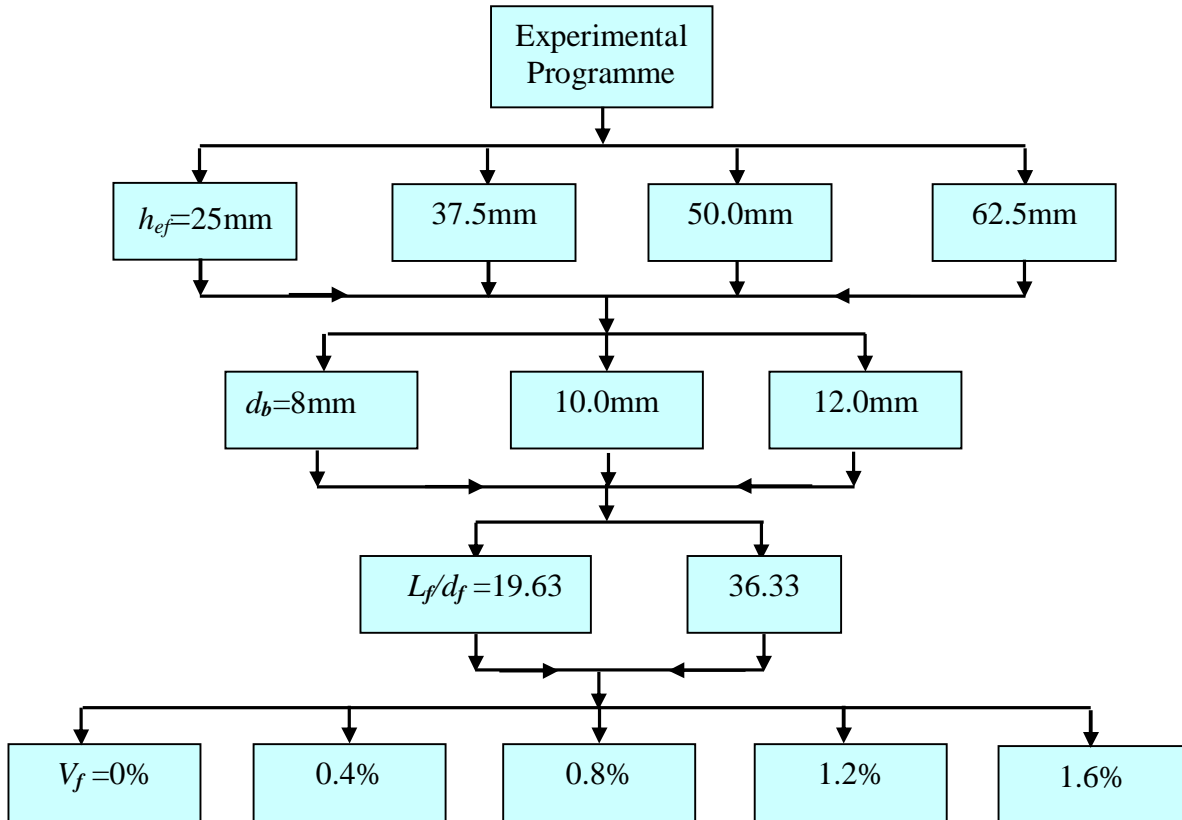

Fig.(2) Flow chart for the experimental programme

Table (1) Properties of the Anchor Bolts.

Material Specification	Grade or Type	d_b (mm)	Yield Strength (MPa)	Tensile Strength (MPa)	Elongation Min. (mm)	Reduction of area Min.(%)
ASTMA307	A	8	414	414	50.8	
ASTmA354	BD	10	862	1034	50.8	40
		12	862	1034	50.8	40

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Table (2) Material properties

Group	Mix proportion	F.M sand	M.A.S Gravel (*mm*)	V_f (%)	l_f/d_f	av. f'_c (MPa)	av. f_{spf} (MPa)	No. of samples
NC	1:1.7:3.5/0.45	2.91	10	0	---	30.0	2.82	6*
*SFRC0.4	1:1.7:3.5/0.45	2.91	10	0.4	19.63	32.2	3.11	6
SFRC0.8	1:1.7:3.5/0.45	2.91	10	0.8	19.63	33.0	3.67	6
SFRC1.2	1:1.7:3.5/0.45	2.91	10	1.2	19.63	34.0	3.38	6
SFRC1.6	1:1.7:3.5/0.45	2.91	10	1.6	19.63	35.1	3.58	6
SFRC0.4	1:1.7:3.5/0.45	2.91	10	0.4	36.33	33.0	3.27	6
SFRC0.8	1:1.7:3.5/0.45	2.91	10	0.8	36.33	33.7	3.44	6
SFRC1.2	1:1.7:3.5/0.45	2.91	10	1.2	36.33	35.5	3.57	6
SFRC1.6	1:1.7:3.5/0.45	2.91	10	1.6	36.33	36.3	3.68	6

av. f'_c = average compressive strength.
av. f_{spf} = average splitting strength.
** = 3samples for compressive, and 3 samples for splitting.

* SFRC0.4 = steel fiber reinforced concrete with volume fraction=0.4%

Concrete: Concrete mix proportions was (1:1.7:3.5/0.45), Ordinary Portland Cement, medium size sand with a fineness modulus (2.91), and gravel with maximum aggregate size (10mm) and water/cement ratio of (0.45). The proportions were chosen to produce a concrete compressive strength of (30MPa) and a slump of (100mm). Harex shelled steel fibers with deformed cross section with lengths (l_f =16, and 32mm) were used which gives aspect ratio of (l_f / d_f =19.63, 36.33) respectively. As shown in table (2).

Volume fraction of the steel fibers (v_f =0.4%. 0.8%, 1.2%, 1.6%) were chosen to avoid balling, and segregation and to get good workable mixes.

The dry materials were mixed first, water then added and the mixing procedure continues till the mix becomes homogeneous and the fibers then fed into the mixer gradually and the mixing procedure continues until the mix becomes homogeneous. The specimens were cast together with the six cylinders and placed on the vibrating table to get a thorough compaction. After casting and vibration, all the specimens were covered with a polythene sheet for 24 hours after which the specimens were stripped from the molds and kept in a water tank and cured for 28 days, till the time of testing at the same age.

TEST PROCEDURE

The apparatus for the pullout test is illustrated in Fig.(4). The test specimen was fixed to the lower end of the test apparatus by the (16mm) bar protruding from the bottom

of the specimens. The anchor bolt was connected to the top moving part of the frame apparatus (free surface testing). After placing the specimen in the test apparatus the pullout load was applied through approximately a constant rate to prevent any dynamic effect during the test [6]. Each bolt was tested monotonically in tension until failure occurs.
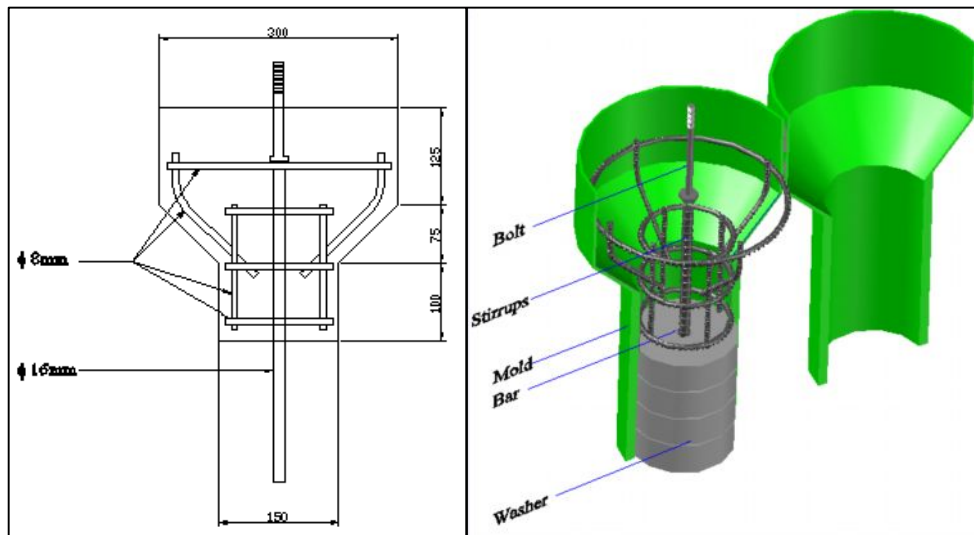
**Fig. (3) Anchorage specimen, (a) Sectional view, (b Three dimensional view.**
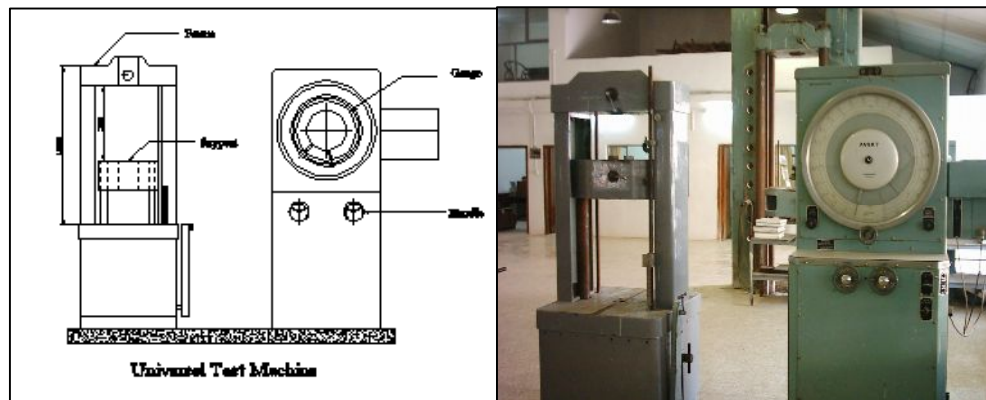
Fig. (4) Test apparatus (Universal Testing Machine).

TEST RESULTS AND DISCUSSION

All the test results are summarized in Table (2). To study the behaviour of headed anchor bolt in tension some parameters will be discussed, such as failure mode,

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effect of the embedment depth, effect of steel fibers volume percentage, and the effect of concrete strength.

Failure mode: Three failure modes were noticed, Fig. (5); (a) the failure shape in (NC) was large concrete failure cone of non uniform shape exceeded the dimensions of the specimen and the cone breaks into pieces in some cases. The angle of the cone ranged between (20-33°). (b) For (SFRC), the failure of the samples having different volume fractions is the same as that for normal concrete, but the concrete failure cone was smaller compared with the cone size in normal concrete, and in the majority of the cases the concrete failure cone was divided into four pieces, such that the angle of failure cannot be easily measured
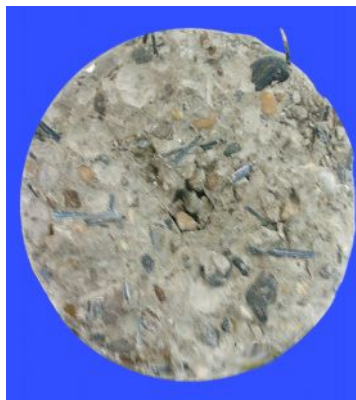
b- Large Failure cone
d_b=10mm, h_{ef}=37.5mm
v_f=1.2%, l_f = 32mm

a -Concrete Failure cone
d_b=8mm, v_f=0%, h_{ef}=25mm

d- Steel Failure, d_b=12mm
v_f=0.4%, l_f=16mm

c -Failure cone with splitting cracks
Bolt did not pullout
d_b=10mm, v_f=0.8%, l_f=16mm

Fig.(5) Typical failure types after test: (a) normal concrete; (b-d) steel fibre Reinforced concrete.

(c) In some cases the failure occurred by splitting cracks on the surface of the specimen, but the bolt did not pullout from the concrete because some fibers remained bonded to the concrete near the head of the anchor and prevented pullout anchor bolt. In some cases the anchor bolts was pulled out from the concrete and some pieces of the cone still connected to the specimen, specially for long fibers (l_f / d_f =36.33). (d) The last mode of failure was yielding and fractures of bolts (steel failure) before pullout of the bolt occur. These cases were excluded from the test results.

Effect of embedment depth: The embedment depth is the main factor influencing the breakout capacity of the different types of anchors [3, 8, and 9]. Fig. (6) Shows the nonlinear increase of breakout capacity with the embedment depth.

When (h_{ef}) increase, the dimensions of the specimen must be increased to at least ($6h_{ef} \times 6h_{ef}$) to avoid the edge effect [9, 10] and the corresponding decrease in the breakout capacity. Angle of failure (θ) decreases when (h_{ef}) increase [1, 8], and the volume of the cone increase when (h_{ef}) increase also [1, 4, 8]. For short embedment depth, the concrete strength appeared to be more effective mainly because shallow anchors failed generally via concrete cone breakout. As the anchor embedment depth was increased, however, this beneficial effect was reduced due to shifting of failure mode of the anchors from concrete failure cone to pullout or steel failure [9].

For (h_{ef}=62.5mm) the amount of increase in the breakout capacity is higher than the others embedment depth (h_{ef}= 25, 37.5, 50mm) because the compressive strength was more than (30MPa) and in some specimens it was up to (40MPa) or more.

Effect of steel fibers: Addition of steel fibers to concrete improves the compressive strength to some extent and the tensile strength to a greater extent. From the test results of the control specimens the increase in the compressive strength for mixes with short fibers (l_f / d_f =19.63) was (6, 8, 12, 15.0%) for (v_f =0.4, 0.8, 1.2, 1.6%) respectively, and the corresponding increase in the splitting tensile strength was (10, 16, 20, 27%). For mixes with long fibers (l_f / d_f =36.33) the increase in the compressive strength was (8, 11, 16,

19%) for (v_f =0.4, 0.8, 1.2, 1.6%) respectively, and the corresponding increase in the splitting tensile strength was (16, 22, 27, 31%). It can be noticed from the pervious results that the increase in the tensile strength for mixes with the long fibers is more than that for mixes with short fibers due to the longer anchorage length [10-12].
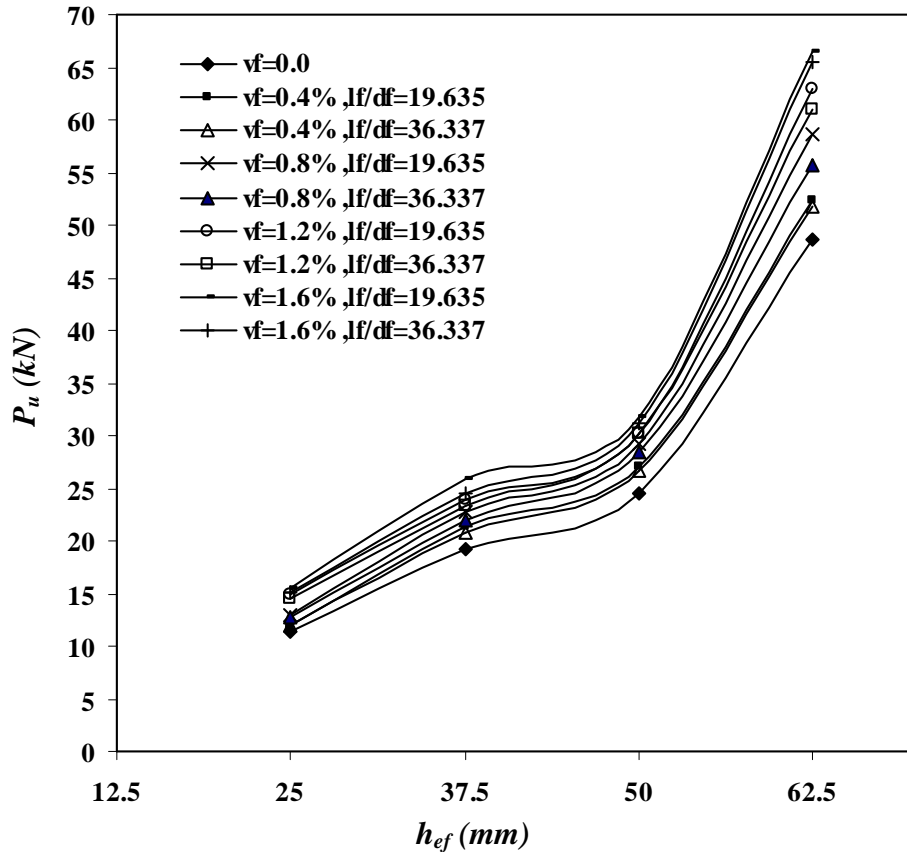
**Fig. (6) Variation of observed breakout capacity(P_u)
with embedment depth(h_{ef}).**

As shown in Fig. (7), the breakout capacity increased significantly with the volume fraction of steel fibers. The Figure shows that the amount of increase in the breakout capacity for anchor bolts embedded in (SFRC) with short steel fiber (l_f / d_f =19.63) was greater than for long fiber (l_f / d_f =36.33). This may be attributed to the fact that the distribution of short fibers in concrete mixes is better than for mixes with long fibers, and for the same volume fraction the number of fibers per unit volume of the matrix are more and the spacing are less between short fibers than those for long fibers [1, 9, 11]. In some cases the difference in breakout capacity values between the two types of fibers was small as shown in Fig.(7).

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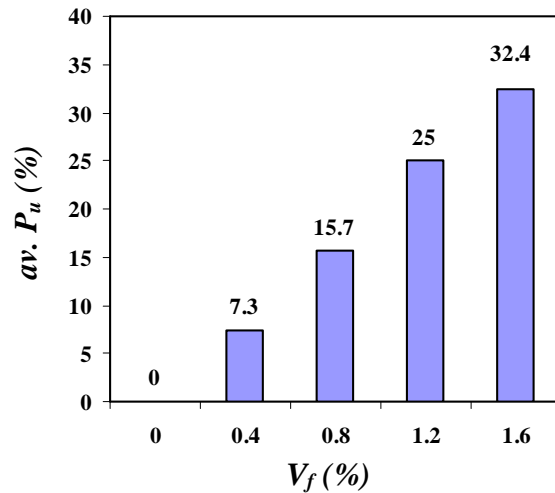
(a)- Average increase in (P_u) with volume fraction of steel fibers (V_f).
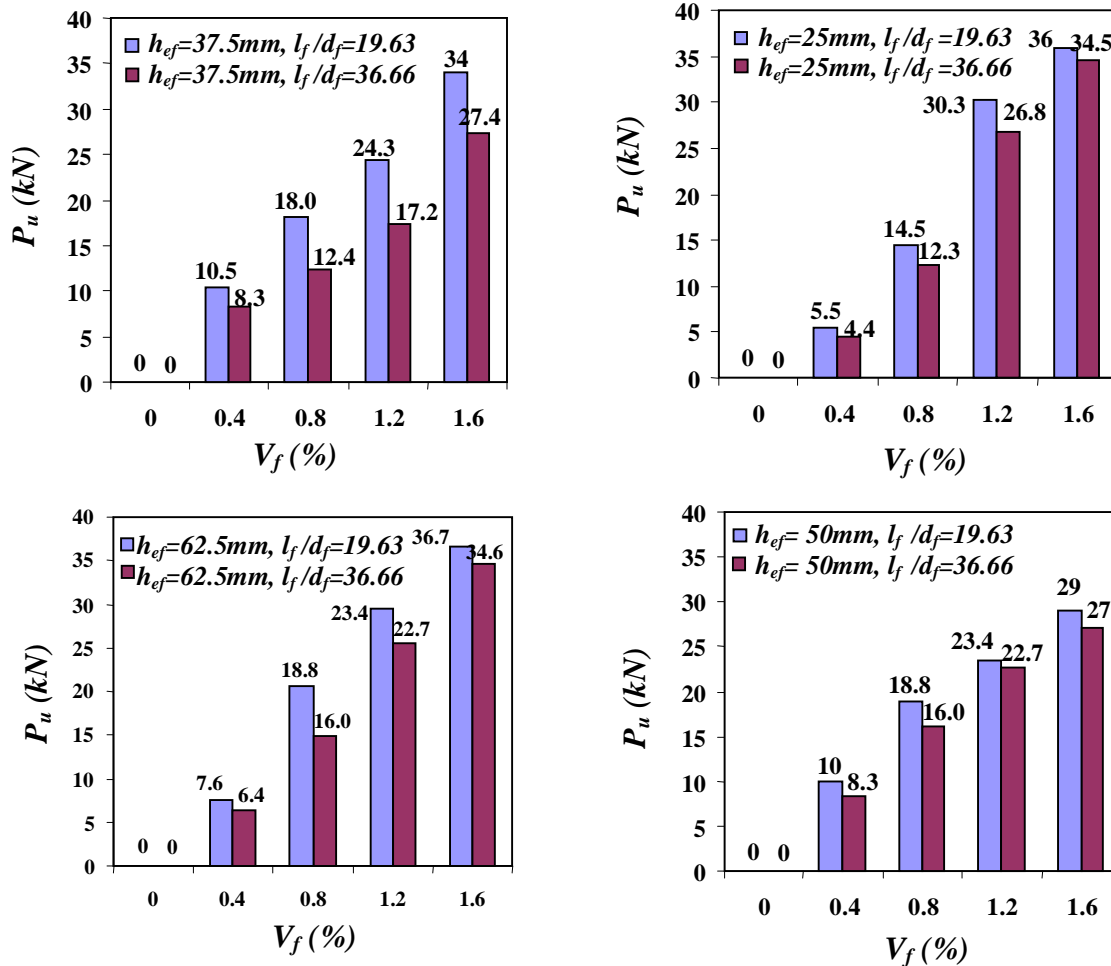
(b)- Variation of observed breakout capacity (P_u) with volume fraction of steel fiber (V_f %)

Fig. (7)Effect of steel fibers on breakout capacity (P_u), (a) Amount of increase, (b) Variation with steel fiber.

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Effect of concrete strength: Generally the anchor capacity increased with the tensile strength of concrete, and the latter increased with the concrete strength [2, 13, 14], even though the increment is not uniform for some cases. Steel fibers enhance the concrete strength, especially the tensile strength depending on the mechanical interlock between the steel fibers and concrete, and the pullout strength of steel fibers. Fig. (8) shows the variation in the anchor capacity with the concrete strength.
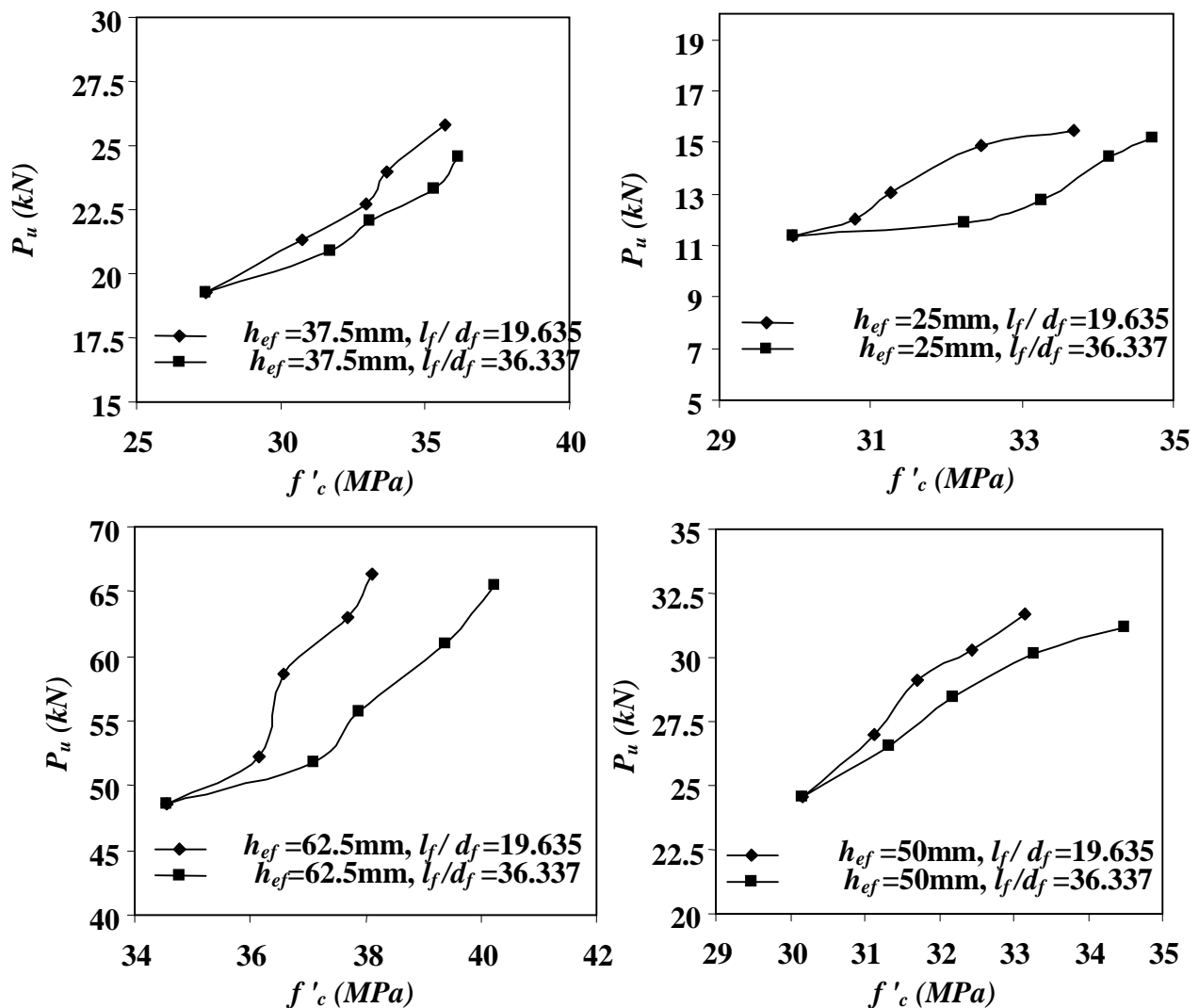
Fig.(8) Variation of the failure load with the compressive strength of concrete.

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Table (2) Test results

No.	Group	h_{ef} (mm)	v_f (%)	l_f/d_f	d_b (mm)	f'_c (MPa)	f_{spf} (MPa)	P_{test} (kN)
1	NC	25	0	0	8	30.0	2.49	11.278
2	NC	25	0	0	10	30.0	2.49	11.376
3	NC	25	0	0	12	30.0	2.49	11474
4	SFRC0.4	25	0.4	19.63	8	30.8	2.97	11.768
5	SFRC0.4	25	0.4	19.63	10	30.8	2.97	12.013
6	SFRC0.4	25	0.4	19.63	12	30.8	2.97	12.258
7	SFRC0.8	25	0.8	19.63	8	31.2	3.12	12.602
8	SFRC0.8	25	0.8	19.63	10	31.2	3.12	12.945
9	SFRC0.8	25	0.8	19.63	12	31.2	3.12	13.533
10	SFRC1.2	25	1.2	19.63	8	32.4	3.22	14.465
11	SFRC1.2	25	1.2	19.63	10	32.4	3.22	14.710
12	SFRC1.2	25	1.2	19.63	12	32.4	3.22	15.298
13	SFRC1.6	25	1.6	19.63	8	33.6	3.55	15.325
14	SFRC1.6	25	1.6	19.63	10	33.6	3.55	15.446
15	SFRC1.6	25	1.6	19.63	12	33.6	3.55	15.642
16	SFRC0.4	25	0.4	36.33	8	32.2	3.21	11.670
17	SFRC0.4	25	0.4	36.33	10	32.2	3.21	11.866
18	SFRC0.4	25	0.4	36.33	12	32.2	3.21	12.097
19	SFRC0.8	25	0.8	36.33	8	32.3	3.35	12.223
20	SFRC0.8	25	0.8	36.33	10	32.3	3.35	12.800
21	SFRC0.8	25	0.8	36.33	12	32.3	3.35	13.310
22	SFRC1.2	25	1.2	36.33	8	34.1	3.44	13.730
23	SFRC1.2	25	1.2	36.33	10	34.1	3.44	14.563
24	SFRC1.2	25	1.2	36.33	12	34.1	3.44	14.980
25	SFRC1.6	25	1.6	36.33	8	34.7	3.57	15.050
26	SFRC1.6	25	1.6	36.33	10	34.7	3.57	15.170
27	SFRC1.6	25	1.6	36.33	12	34.7	3.57	15.290
28	NC	37.5	0	0	8	27.4	2.48	18.926
29	NC	37.5	0	0	10	27.4	2.48	19.240
30	NC	37.5	0	0	12	27.4	2.48	19.654
31	SFRC0.4	37.5	0.4	19.63	8	30.7	2.83	20.775
32	SFRC0.4	37.5	0.4	19.63	10	30.7	2.83	21.304
33	SFRC0.4	37.5	0.4	19.63	12	30.7	2.83	21.832
34	SFRC0.8	37.5	0.8	19.63	8	32.9	3.16	22.316
35	SFRC0.8	37.5	0.8	19.63	10	32.9	3.16	22.875
36	SFRC0.8	37.5	0.8	19.63	12	32.9	3.16	23.065
37	SFRC1.2	37.5	1.2	19.63	8	33.6	3.34	23.677
38	SFRC1.2	37.5	1.2	19.63	10	33.6	3.34	23.987
39	SFRC1.2	37.5	1.2	19.63	12	33.6	3.34	24.251
40	SFRC1.6	37.5	1.6	19.63	8	35.7	3.49	25.068
41	SFRC1.6	37.5	1.6	19.63	10	35.7	3.49	25.887
42	SFRC1.6	37.5	1.6	19.63	12	35.7	3.49	26.571
43	SFRC0.4	37.5	0.4	36.33	8	31.5	2.94	20.256
44	SFRC0.4	37.5	0.4	36.33	10	31.5	2.94	20.937
45	SFRC0.4	37.5	0.4	36.33	12	31.5	2.94	21.447

46	SFRC0.8	37.5	0.8	36.33	8	33.0	3.32	21.625
47	SFRC0.8	37.5	0.8	36.33	10	33.0	3.32	21.975
48	SFRC0.8	37.5	0.8	36.33	12	33.0	3.32	22.565
49	SFRC1.2	37.5	1.2	36.33	8	35.3	3.51	22.876
50	SFRC1.2	37.5	1.2	36.33	10	35.3	3.51	23.256
51	SFRC1.2	37.5	1.2	36.33	12	35.3	3.51	23.768
52	SFRC1.6	37.5	1.6	36.33	8	36.1	3.56	24.125
53	SFRC1.6	37.5	1.6	36.33	10	36.1	3.56	24.563
54	SFRC1.6	37.5	1.6	36.33	12	36.1	3.56	25.000
55	NC	50	0	0	8	30.1	2.79	24.419
56	NC	50	0	0	10	30.1	2.79	24.517
57	NC	50	0	0	12	30.1	2.79	24.664
58	SFRC0.4	50	0.4	19.63	8	31.1	3.01	***
59	SFRC0.4	50	0.4	19.63	10	31.1	3.01	26.871
60	SFRC0.4	50	0.4	19.63	12	31.1	3.01	27.145
61	SFRC0.8	50	0.8	19.63	8	31.7	3.11	***
62	SFRC0.8	50	0.8	19.63	10	31.7	3.11	28.930
63	SFRC0.8	50	0.8	19.63	12	31.7	3.11	29.372
64	SFRC1.2	50	1.2	19.63	8	32.4	3.20	***
65	SFRC1.2	50	1.2	19.63	10	32.4	3.20	30.166
66	SFRC1.2	50	1.2	19.63	12	32.4	3.20	30.400
67	SFRC1.6	50	1.6	19.63	8	33.1	3.46	***
68	SFRC1.6	50	1.6	19.63	10	33.1	3.46	31.530
69	SFRC1.6	50	1.6	19.63	12	33.1	3.46	31.804
70	SFRC0.4	50	0.4	36.33	8	31.3	3.20	26.135
71	SFRC0.4	50	0.4	36.33	10	31.3	3.20	26.538
72	SFRC0.4	50	0.4	36.33	12	31.3	3.20	27.060
73	SFRC0.8	50	0.8	36.33	8	32.1	3.33	***
74	SFRC0.8	50	0.8	36.33	10	32.1	3.33	28.342
75	SFRC0.8	50	0.8	36.33	12	32.1	3.33	28.587
76	SFRC1.2	50	1.2	36.33	8	33.2	3.41	***
77	SFRC1.2	50	1.2	36.33	10	33.2	3.41	29.975
78	SFRC1.2	50	1.2	36.33	12	33.2	3.41	30.264
79	SFRC1.6	50	1.6	36.33	8	34.4	3.55	***
80	SFRC1.6	50	1.6	36.33	10	34.4	3.55	30.940
81	SFRC1.6	50	1.6	36.33	12	34.4	3.55	31.382
82	NC	62.5	0	0	8	34.5	3.35	***
83	NC	62.5	0	0	10	34.5	3.35	48.277
84	NC	62.5	0	0	12	34.5	3.35	48.885
85	SFRC0.4	62.5	0.4	19.63	8	36.1	3.61	***
86	SFRC0.4	62.5	0.4	19.63	10	36.1	3.61	52.285
87	SFRC0.4	62.5	0.4	19.63	12	36.1	3.61	***
88	SFRC0.8	62.5	0.8	19.63	8	36.5	3.68	***
89	SFRC0.8	62.5	0.8	19.63	10	36.5	3.68	***
90	SFRC0.8	62.5	0.8	19.63	12	36.5	3.68	58.577
91	SFRC1.2	62.5	1.2	19.63	8	37.6	3.77	***
92	SFRC1.2	62.5	1.2	19.63	10	37.6	3.77	62.435
93	SFRC1.2	62.5	1.2	19.63	12	37.6	3.77	63.481
94	SFRC1.6	62.5	1.6	19.63	8	38.1	3.84	***

95	SFRC1.6	62.5	1.6	19.63	10	38.1	3.84	66.364
96	SFRC1.6	62.5	1.6	19.63	12	38.1	3.84	66.491
97	SFRC0.4	62.5	0.4	36.33	8	37.0	3.74	***
98	SFRC0.4	62.5	0.4	36.33	10	37.0	3.74	51.587
99	SFRC0.4	62.5	0.4	36.33	12	37.0	3.74	51.863
100	SFRC0.8	62.5	0.8	36.33	8	37.8	3.78	***
101	SFRC0.8	62.5	0.8	36.33	10	37.8	3.78	55.479
102	SFRC0.8	62.5	0.8	36.33	12	37.8	3.78	56.048
103	SFRC1.2	62.5	1.2	36.33	8	39.3	3.92	***
104	SFRC1.2	62.5	1.2	36.33	10	39.3	3.92	60.475
105	SFRC1.2	62.5	1.2	36.33	12	39.3	3.92	61.496
106	SFRC1.6	62.5	1.6	36.33	8	40.2	4.05	***
107	SFRC1.6	62.5	1.6	36.33	10	40.2	4.05	65.167
108	SFRC1.6	62.5	1.6	36.33	12	40.2	4.05	65.687

*** Steel failure

CONCLUSIONS

The breakout capacity of headed anchor bolts embedded in concrete increased almost linearly with the volume fraction of the added steel fibers by up to 32%. The increase in the breakout capacity was found to be more for short fibers than for long fibers. The volume of the failure concrete cone for headed bolts embedded in fibrous concrete is less than that for headed bolts embedded in plain or unreinforced concrete. More experimental results are required to verify these findings and to develop a method for predicting the breakout capacity of headed bolts embedded in fibrous concrete.

NOTATIONS

v_f *Volume fraction of steel fibers (%)*
l_f / d_f *Aspect ratio (fiber length/fiber diameter)*
d_b *diameter of bolt (mm)*
h_{ef} *Embedment depth (mm)*
P_u *Observed breakout capacity (Failure load)*
f_c' *Compressive strength (MPa)*
f_{sp}' *Splitting strength (MPa)*

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